

### 4.3 Problems

**Problem 1.** Approximate  $\int_0^{.5} \frac{2}{x-4} dx$  using (a) trapezoidal rule (b) Simpson's rule (c) midpoint rule. Bound the error, and compare that to the actual error.

**Problem 2.** The Trapezoidal rule applied to  $\int_0^2 f(x) dx$  gives the value 4, and Simpson's rule gives the value 2. What is  $f(1)$ ?

**Problem 3.** Find the constants  $c_0, c_1, x_1$  so that the quadrature formula  $\int_0^1 f(x) dx = c_0 f(0) + c_1 f(x_1)$  has the highest possible degree of precision.

### 4.4 Problems

**Problem 4.** Determine the values of  $n$  and  $h$  required to approximate  $\int_0^2 e^{2x} \sin(3x) dx$  to within  $10^{-4}$  using (a) composite trapezoidal rule (b) composite Simpson's rule (c) composite midpoint rule.

### 4.5 Problems

**Problem 5.** Use Romberg integration to compute  $R_{3,3}$  for  $\int_1^{1.5} x^2 \ln(x) dx$